

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel**  
**International**  
**Advanced Level**

Centre Number

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Candidate Number

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**Monday 8 June 2020**

Morning (Time: 1 hour 30 minutes)

Paper Reference **WFM03/01**

**Mathematics**

**International Advanced Subsidiary/Advanced Level**  
**Further Pure Mathematics F3**

**You must have:**

Mathematical Formulae and Statistical Tables (Blue), calculator

Total Marks

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**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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2. Determine

(i)  $\int \frac{1}{3x^2 + 12x + 24} dx$  (4)

(ii)  $\int \frac{1}{\sqrt{27 - 6x - x^2}} dx$  (4)

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Question 4 continued

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Q4

(Total 9 marks)

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6.

$$\mathbf{A} = \begin{pmatrix} 1 & -1 & 1 \\ 1 & 1 & 1 \\ 1 & 2 & a \end{pmatrix} \quad a \neq 1$$

(a) Find  $\mathbf{A}^{-1}$  in terms of  $a$ .

(4)

$$\mathbf{B} = \begin{pmatrix} 1 & -1 & 1 \\ 1 & 1 & 1 \\ 1 & 2 & 4 \end{pmatrix}$$

The straight line  $l_1$  is mapped onto the straight line  $l_2$  by the transformation represented by the matrix  $\mathbf{B}$ .

The equation of  $l_2$  is

$$(\mathbf{r} - (12\mathbf{i} + 4\mathbf{j} + 6\mathbf{k})) \times (-6\mathbf{i} + 2\mathbf{j} + 3\mathbf{k}) = \mathbf{0}$$

(b) Find a vector equation for the line  $l_1$ 

(4)

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Question 6 continued

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**Question 6 continued**

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7. The curve  $C$  has parametric equations

$$x = \cosh t + t, \quad y = \cosh t - t \quad 0 \leq t \leq \ln 3$$

(a) Show that

$$\left(\frac{dx}{dt}\right)^2 + \left(\frac{dy}{dt}\right)^2 = 2 \cosh^2 t \tag{3}$$

The curve  $C$  is rotated through  $2\pi$  radians about the  $x$ -axis. The area of the curved surface generated is given by  $S$ .

(b) Show that

$$S = 2\pi\sqrt{2} \int_0^{\ln 3} (\cosh^2 t - t \cosh t) dt \tag{2}$$

(c) Hence find the value of  $S$ , giving your answer in the form

$$\frac{\pi\sqrt{2}}{9}(a + b \ln 3)$$

where  $a$  and  $b$  are constants to be determined. (7)

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